

# Fatigue Life Prediction of Complex 2D Components under Mixed-Mode Variable Loading

M.A. Meggiolaro<sup>1</sup>, A.C.O. Miranda<sup>2</sup>, J.T.P. Castro<sup>1</sup>, L.F. Martha<sup>\*2</sup>, T.N. Bittencourt<sup>3</sup>

<sup>1</sup>Department of Mechanical Engineering and <sup>2</sup>Department of Civil Engineering

Pontifical Catholic University of Rio de Janeiro (PUC-Rio), Rio de Janeiro, RJ - 22453-900 Brazil

<sup>3</sup>Computational Mechanics Laboratory, Department of Structures and Foundations Engineering, Polytechnic School at the University of São Paulo, PO Box 61548, São Paulo, SP - 05424-970 - Brazil  
tels: (5521)9764-2866, (5521)2511-5846, fax: (5521)3114-1165

e-mails: meggi@mec.puc-rio.br, amiranda@tecgraf.puc-rio.br, jtcastro@mec.puc-rio.br,  
lfm@civ.puc-rio.br, tbitten@usp.br

## Abstract

In defect-tolerant structures, accurate fatigue crack propagation and residual strength predictions under variable amplitude loading are essential to maximize the required time between inspections, minimizing costs. However, such task is not trivial for real structural components, which generally have complex geometries with cracks that may change direction due to mixed-mode loading. The use of global Finite Element (FE) software to predict both crack path and crack growth rate is not computationally efficient, because variable amplitude loading would require time-consuming remeshing at each propagation cycle. In this work, a two-phase methodology that is both precise and cost effective is presented, based on two pieces of software to numerically predict fatigue crack growth. First, the fatigue crack path and its stress intensity factor are calculated in a specialized (global) FE program, using fixed crack increments, resulting in only a few required remeshing steps. Numerical methods are used to calculate the crack propagation path, based on the computation of the crack incremental direction, and the stress-intensity factors  $K_I$ , from the finite element response. Then, an analytical expression is fitted to the calculated  $K_I(\mathbf{a})$  values, where  $\mathbf{a}$  is the length along the crack path. This  $K_I(\mathbf{a})$  expression is used as an input to a powerful general purpose fatigue design program based in the local approach. This (local) software has been developed to predict both initiation and propagation fatigue lives under variable loading, considering load interaction effects such as crack retardation or acceleration after overloads. This methodology is numerically and experimentally validated by benchmark tests of fatigue crack propagation in complex two-dimensional structural components. Cracks are fatigue propagated under variable amplitude loading in standard SEN and CTS specimens and on panels with oblique cracks, all with holes specially positioned to attract or to deflect the cracks. It is found that the combination of both global and local software is able to predict the (curved) crack path and remaining life in each case, even considering load interaction effects.

- [1] Miranda, A. C. O., Meggiolaro, M. A., Castro, J. T. P., Martha, L. F. and Bittencourt, T. N., "Fatigue Crack Propagation under Complex Loading in Arbitrary 2D Geometries," Applications of Automation Technology in Fatigue and Fracture Testing and Analysis, *ASTM STP 1411*, A. A. Braun et al., Eds., ASTM, 2002.

\* presenting author (lfm@civ.puc-rio.br)

[P11]

# Fatigue Life Prediction of Complex 2D Components under Mixed-Mode Variable Loading

**Marco Antonio Meggiolaro<sup>1</sup>**

**Antonio Carlos de Oliveira Miranda<sup>2</sup>**

**Jaime Tupiassú Pinho de Castro<sup>1</sup>**

**Luiz Fernando Martha<sup>2</sup>**

**Tulio N. Bittencourt<sup>3</sup>**

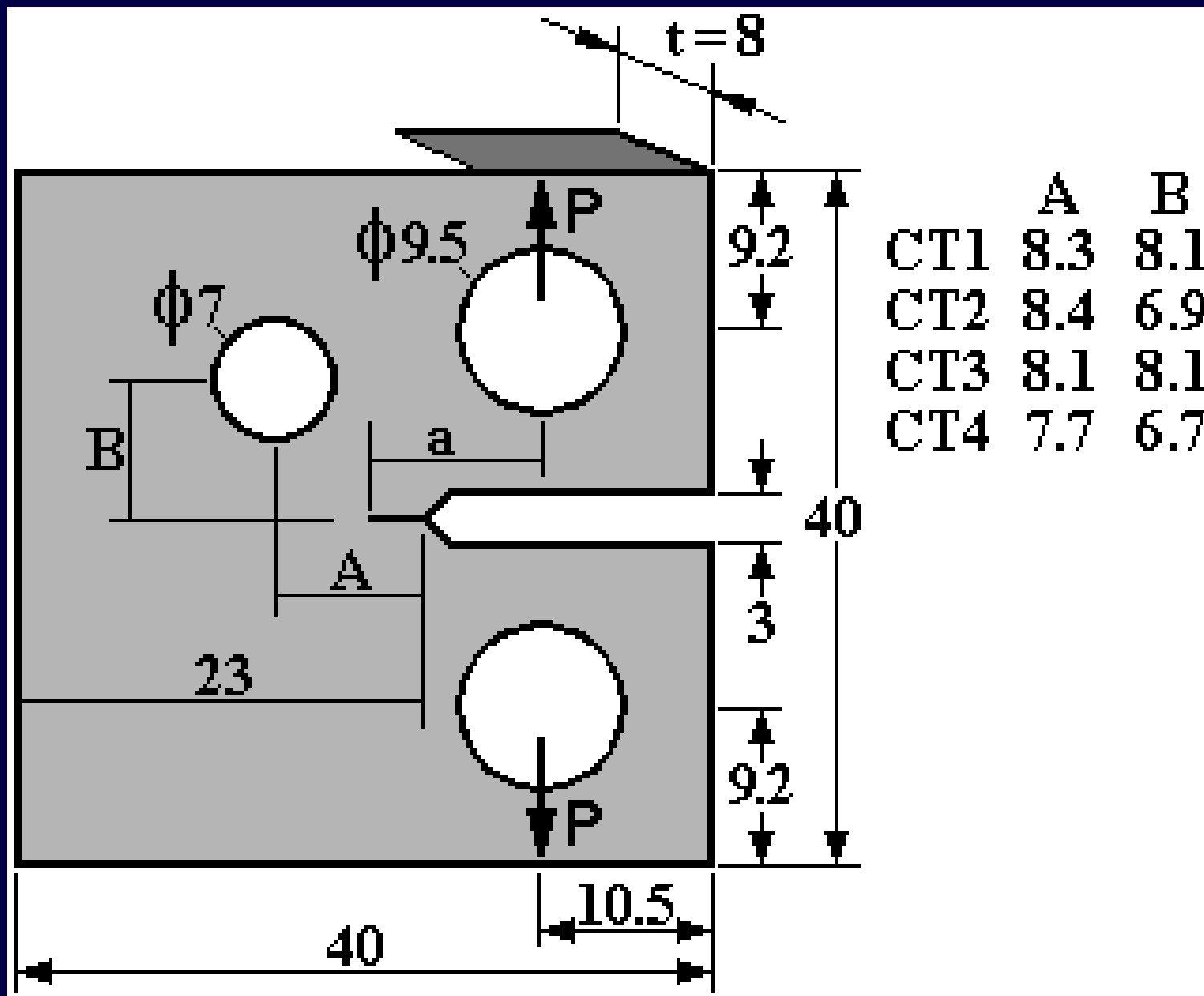
<sup>1</sup>Mechanical Engineering Dept., PUC-Rio, Rio de Janeiro, Brazil

<sup>2</sup>Civil Engineering Dept., PUC-Rio, Rio de Janeiro, Brazil

<sup>3</sup>Computational Mechanics Laboratory, USP, São Paulo, Brazil

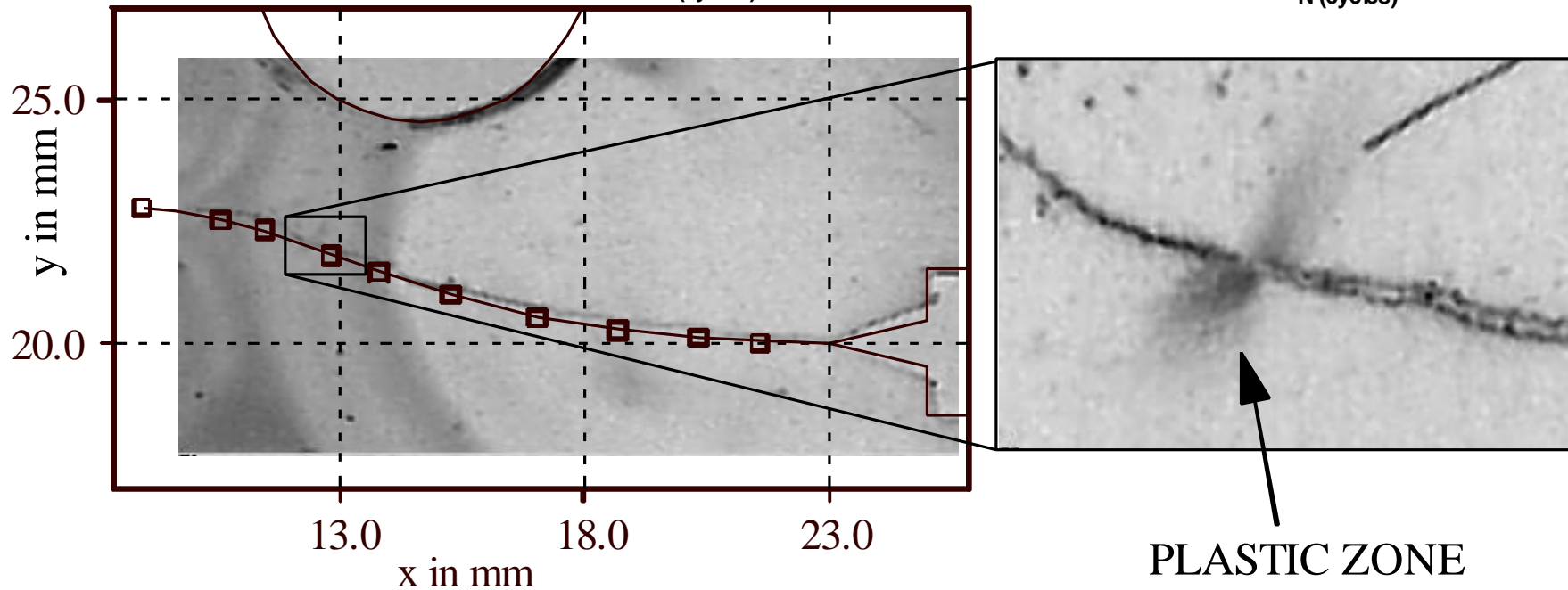
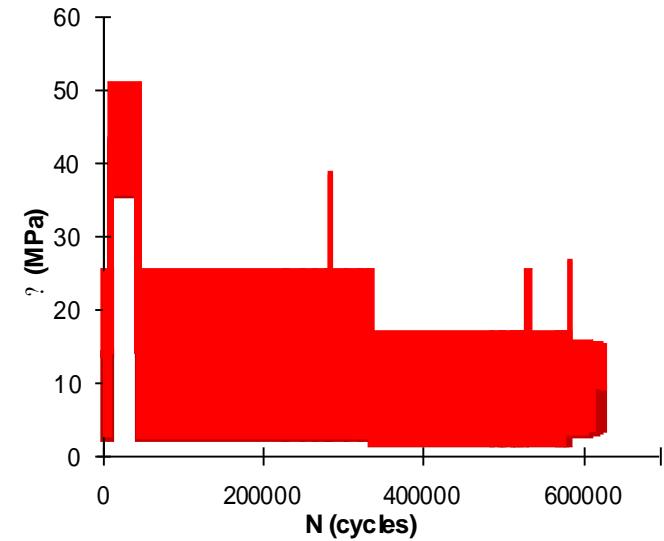
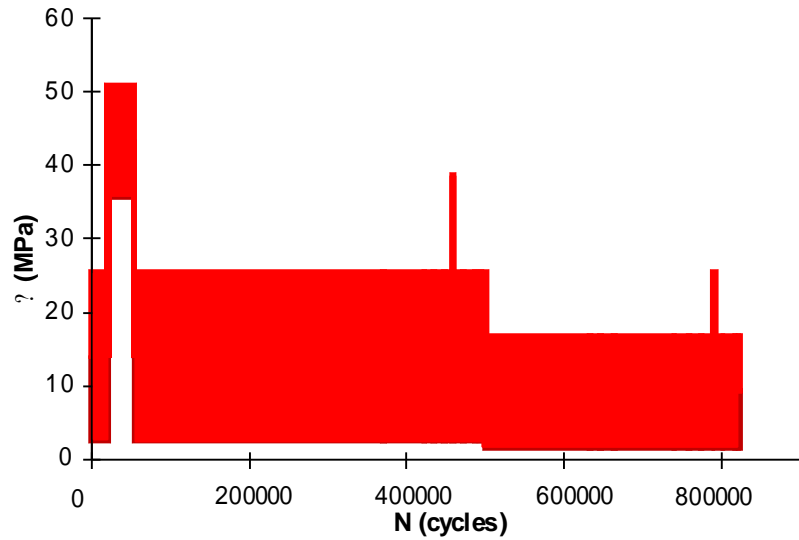
# Software Development to Automate Fatigue Design

- a software named **V i D a** was developed to automate fatigue design by all *local* methods, including *load interaction effects*
- a **FE** companion software called **Quebra2D** predicts the *curved crack path* in *arbitrary 2D geometries*, calculating its associated  **$K_I(\mathbf{a})$**
- this approach is experimentally validated by *fatigue crack propagation* tests under *variable amplitude loading* in standard CT specimens with *holes* specially positioned to attract or to deflect the cracks

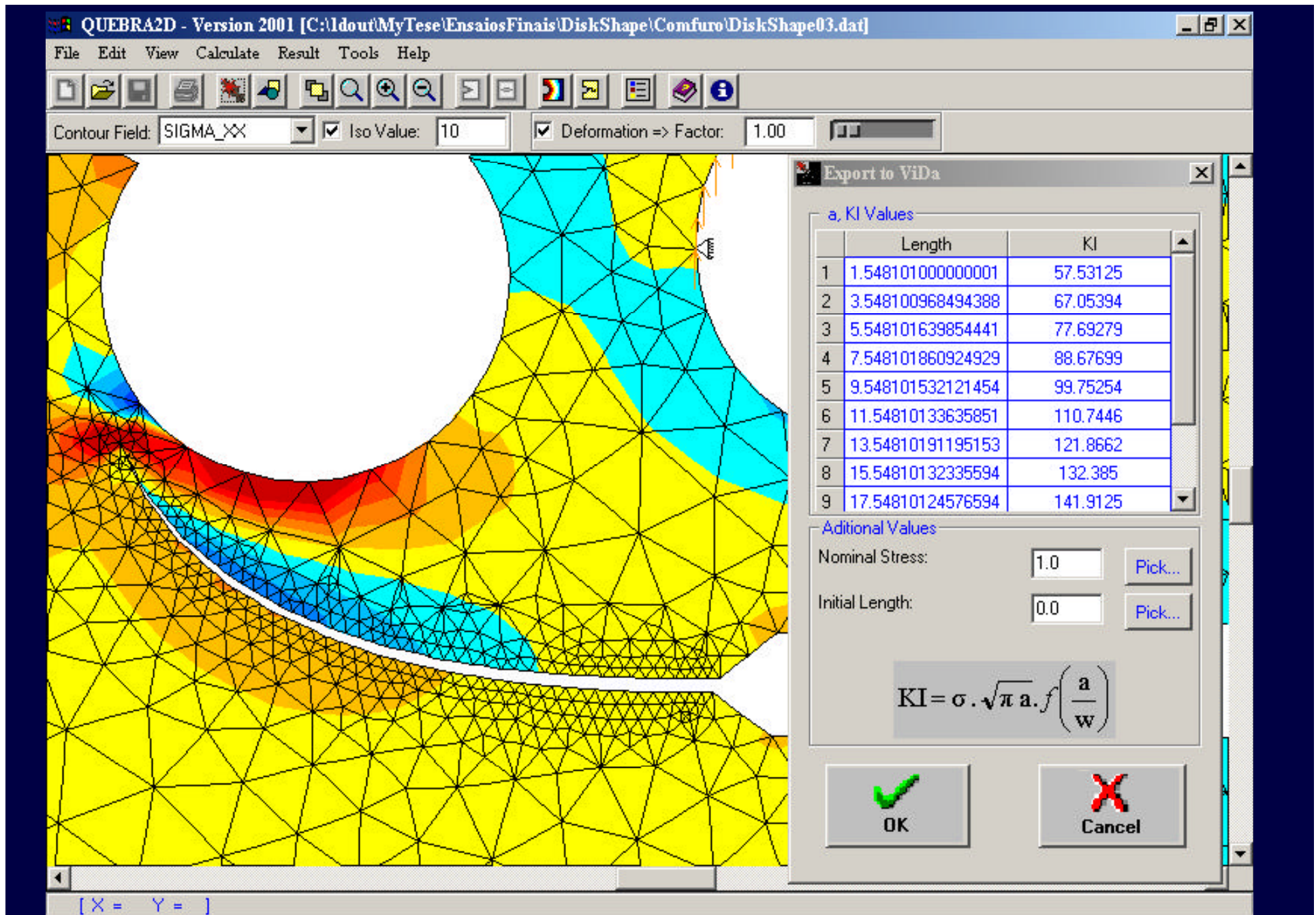


- holed CTS for the *engineered* experiments

applied  
load  
histories:



- the *real* and the *predicted* crack paths, and detail of an overload plastic zone



- screen output of the **Quebra2D** (*global*) software

ViDa 2002 - Visual Damagemeter for Windows - [C:\Idout\MyTese\EnsaioFinais\NewCTS\NewCTS-CP02.a1d]

File Edit View Data Life Tools Window Help

Sy=+000 Su=+000 Klc=250 ==> Aco 1020. Duran

**Crack Growth (da/dN)**

Calculation title :

**da/dN Curve** **Crack** **Retardation/Options**

Initial Crack (a) : 8.40E+00 mm  
 Final Value : a = 0.00E+00 mm

(if Final Value=0 criterion is ignored)  
 Width (w) : 2.95E+01 mm

**disc single-edge crack - Splitting force**

— beta(a)

**Typical** **Database** **Charted**

Inf. strip single-edge crack - Splitting forces (CT-specimen)  
 [a,w,2h=1.25w,a/w>0.2,0.5%]

$$K_I = \frac{P}{t\sqrt{w}} \cdot \frac{(2 + \frac{a}{w})}{(1 - \frac{a}{w})^{1.5}}$$

$$\cdot [ .886 + 4.64 \frac{a}{w} - 13.32 (\frac{a}{w})^2 + 14.72 (\frac{a}{w})^3 - 5.6 (\frac{a}{w})^4 ]$$

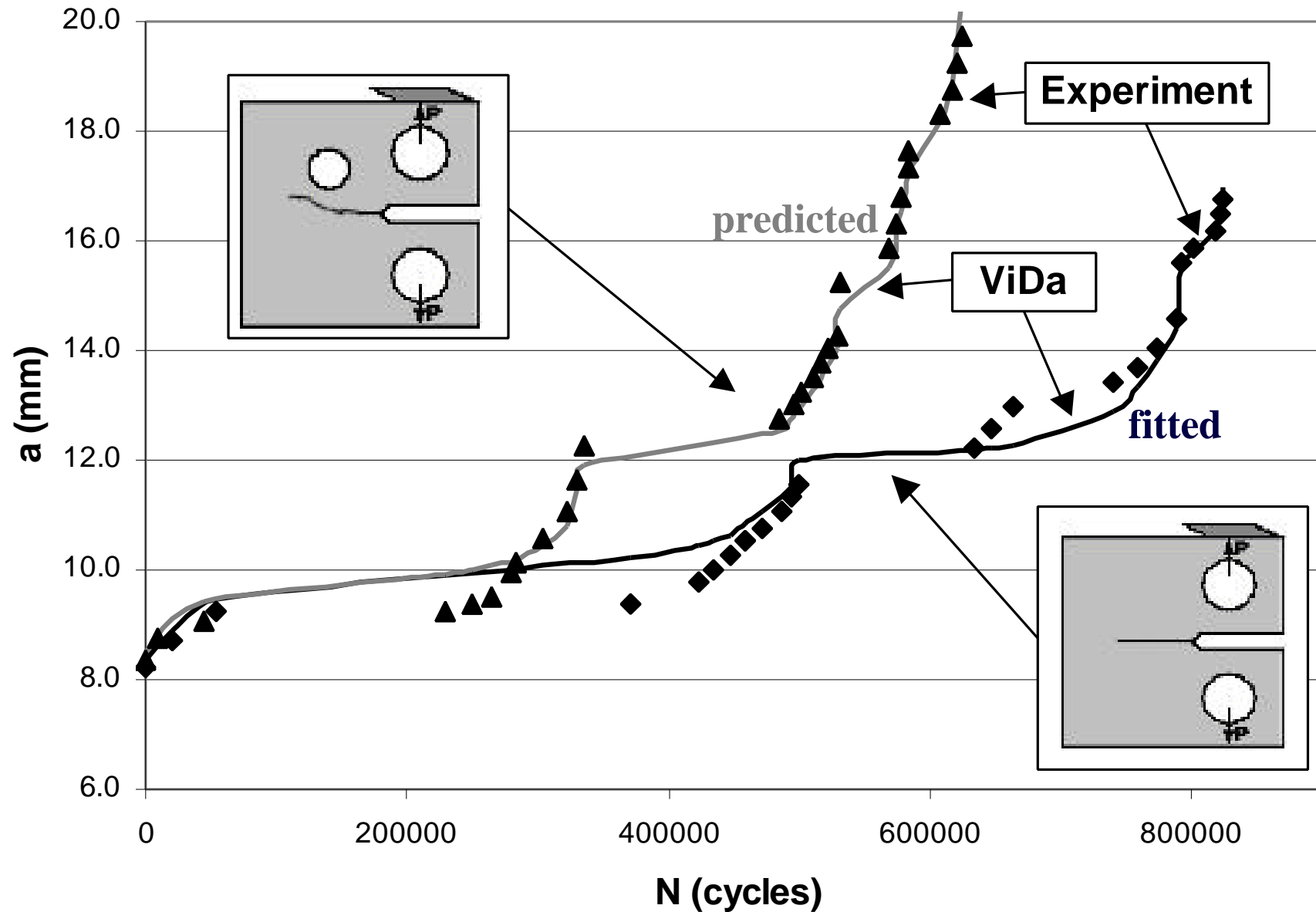
KI    KI,III

A: 8.36E-09    H: 5.00E-01    r: 5.00E+00    z: 8.00E-01  
 b: 1.00E+02    l: 1.00E+00    s: 1.00E+00  
 B: 1.30E+02    L: -5.00E-01    t: 2.00E+01  
 d: 5.00E+02    m: 3.08E+00    v: 3.00E+01  
 D: 1.00E+03    n: 1.00E+00    x: 1.00E+00  
 h: 1.00E+01    p: 6.00E-01    y: 3.50E+00

Open Save OK Cancel

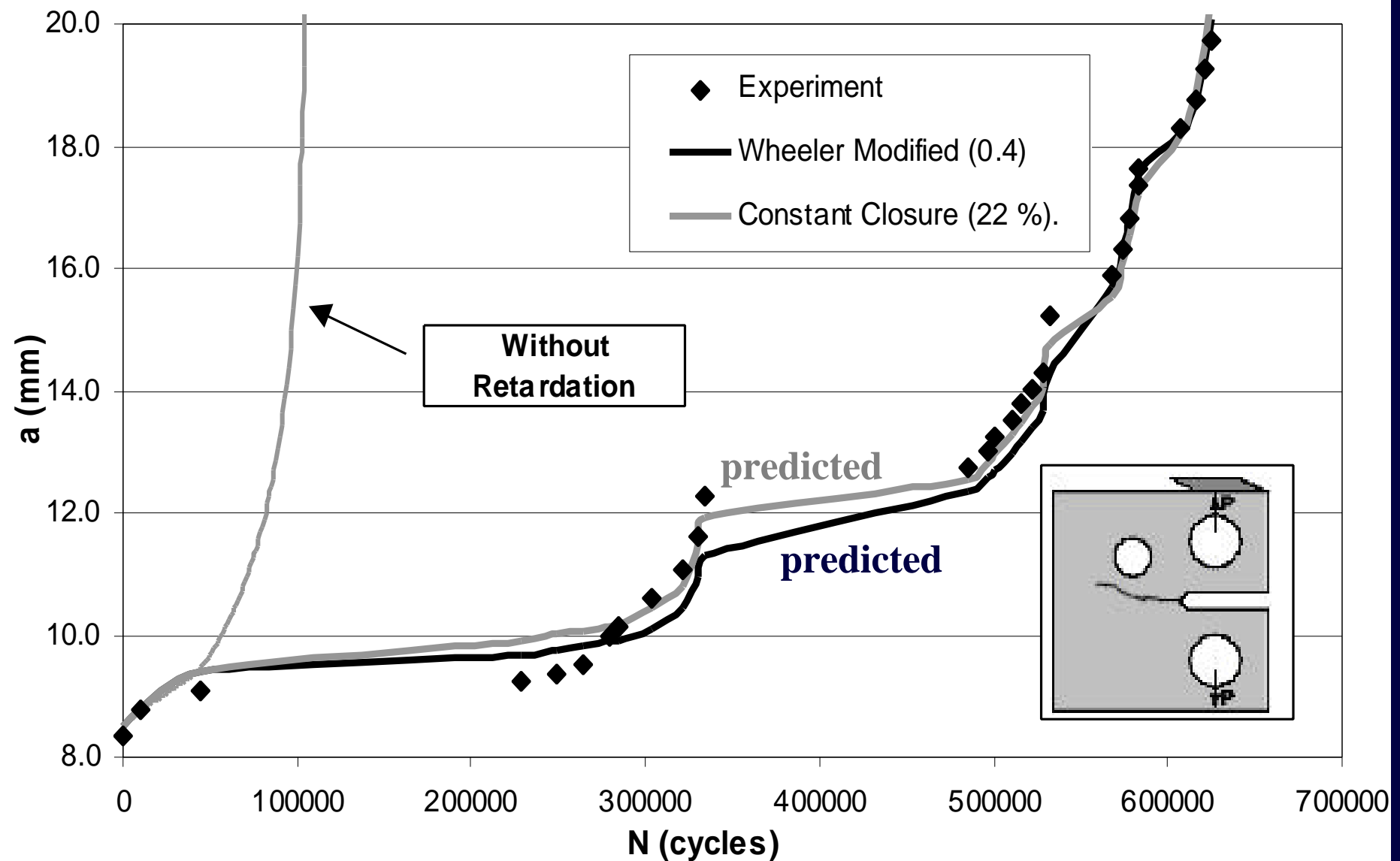
Status

- screen output of the **ViDa** (*local*) software

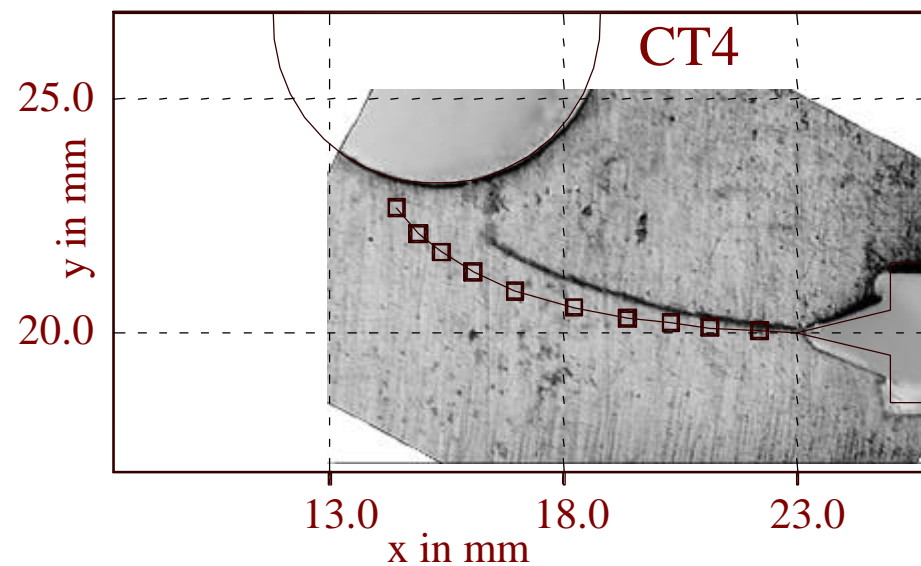
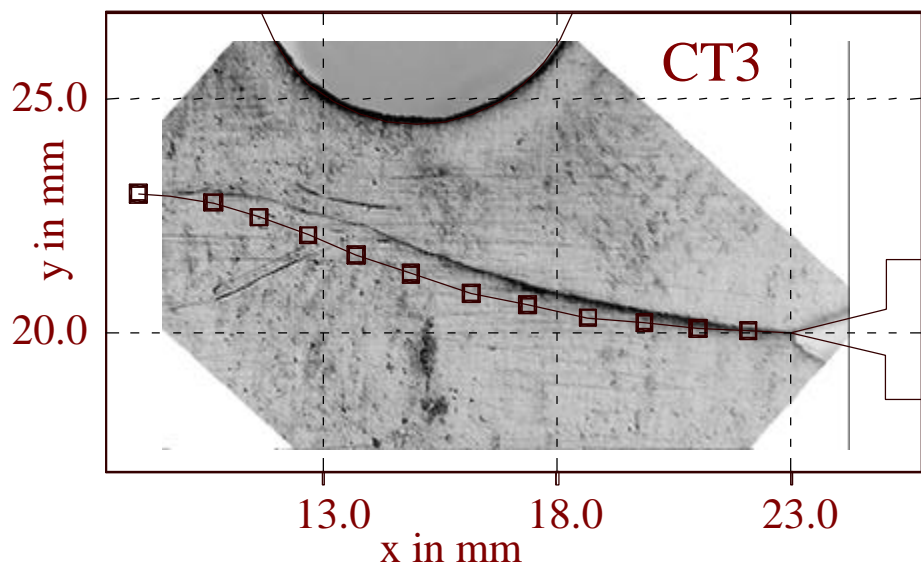
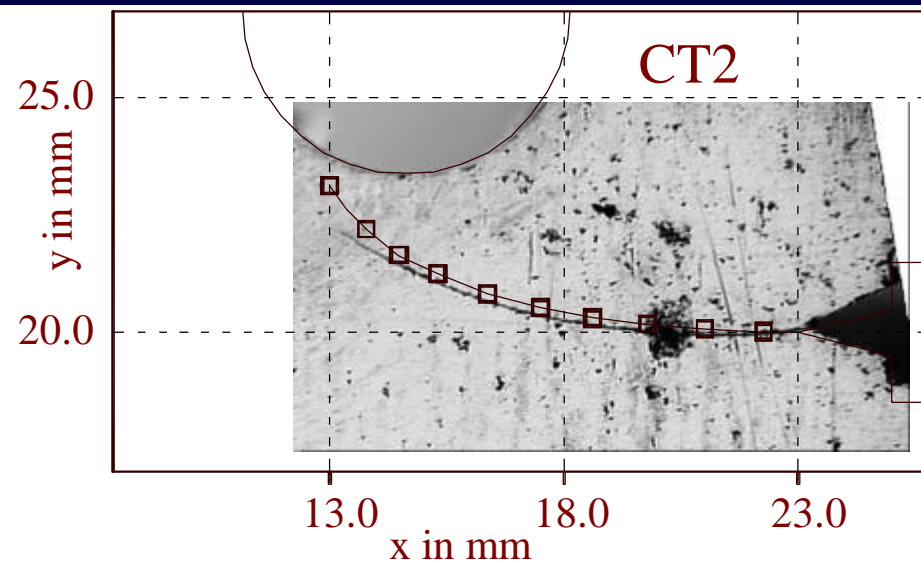
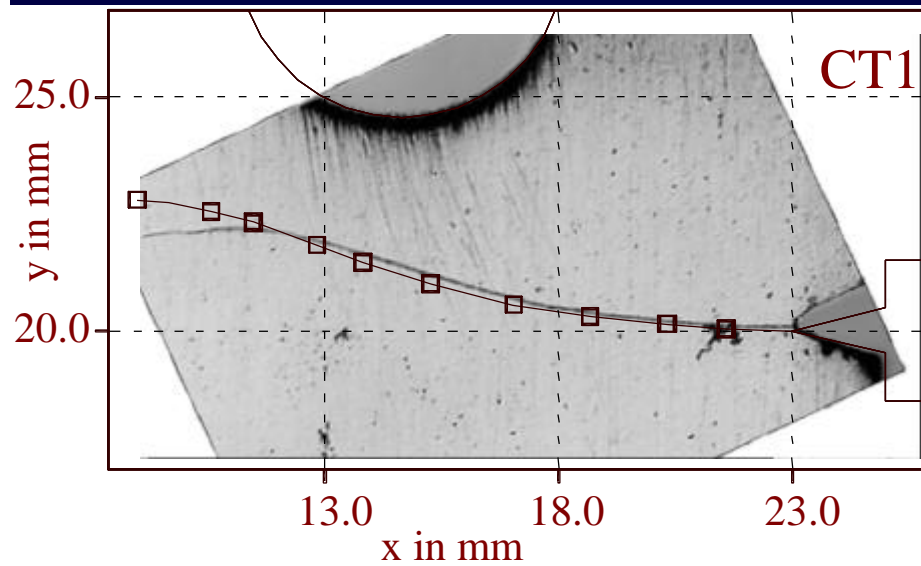


• *predicted* and *measured* crack sizes on holed and standard CTs submitted to *variable amplitude loads*





- *measured* crack sizes on holed CTs and *Constant Closure* and *Modified Wheeler predictions*



—□— FINITE ELEMENT METHOD

- the *experimental* and the *predicted* crack paths

# Conclusions

- the combination of both *global* (**Quebra2D**) and *local* (**V i D a**) software is able to predict the *curved* crack path and remaining life in *complex structures*, even considering *load interaction effects*

- **Reference:**

Miranda, ACO, Meggiolaro, MA, Castro, JTP, Martha, LF and Bittencourt, TN, "Fatigue Crack Propagation under Complex Loading in Arbitrary 2D Geometries," Applications of Automation Technology in Fatigue and Fracture Testing and Analysis, *ASTM STP 1411*, A. A. Braun et al., Eds., ASTM, 2002

## Fatigue Life Prediction of Complex 2D Components under Mixed-Mode Variable Loading

M.A. Meggiolaro<sup>1</sup>, A.C.O. Miranda, J.T.P. Castro<sup>1</sup>, L.F. Martha, T.N. Bittencourt<sup>2</sup>

<sup>1</sup>Pontifical Catholic University of Rio de Janeiro, Rio de Janeiro, Brazil

<sup>2</sup>Polytechnic School at the University of São Paulo, São Paulo, Brazil

In defect-tolerant structures, accurate fatigue crack propagation and residual strength predictions under variable amplitude loading are essential to maximize the required time between inspections, minimizing costs. However, such task is not trivial for real structural components, which generally have complex geometries with cracks that may change direction due to mixed-mode loading. The use of global Finite Element (FE) software to predict both crack path and crack growth rate is not computationally efficient, because variable amplitude loading would require time-consuming remeshing at each propagation cycle. In this work, a two-phase methodology that is both precise and cost-effective is presented, based on two pieces of software to numerically predict fatigue crack growth. First, the fatigue crack path and its stress intensity factor are calculated in a specialized (global) FE program, using fixed crack increments, resulting in only a few required remeshing steps. Numerical methods are used to calculate the crack propagation path, based on the computation of the crack incremental direction due to mixed-mode loading, and the stress-intensity factors  $K_I$  from the FE response. Then, an analytical expression is fitted to the calculated  $K_I(\mathbf{a})$  values, where  $\mathbf{a}$  is the length along the crack path. This  $K_I(\mathbf{a})$  expression is used as an input to a powerful general-purpose fatigue design program based in the local approach. This (local) software has been developed to predict both initiation and propagation fatigue lives under variable loading, considering load interaction effects such as crack retardation or acceleration after overloads. This methodology is numerically and experimentally validated by benchmark tests of fatigue crack propagation in complex two-dimensional structural components. Cracks are fatigue propagated under variable amplitude loading in standard SEN and CTS specimens and on panels with oblique cracks, all with holes specially positioned to attract or to deflect the cracks. It is found that the combination of both global and local software is able to predict the (curved) crack path and remaining life in each case, even considering load interaction effects.

- [1] Miranda, A.C.O., Meggiolaro, M.A., Castro, J.T.P., Martha, L.F. and Bittencourt, T.N. Fatigue Crack Propagation under Complex Loading in Arbitrary 2D Geometries. Applications of Automation Technology in Fatigue and Fracture Testing and Analysis; ASTM STP 1411, A. A. Braun et al., Eds., ASTM, 2002.

Keywords: fatigue crack growth, finite elements, arbitrary geometry, variable loading.